

TRANSFER OF EXTREME RISK BETWEEN SELECTED EU WHEAT MARKETS

Małgorzata Just, PhD¹

Faculty of Economics and Social Sciences, Poznań University of Life Sciences

ABSTRACT

The aim of this study was to analyse the transfer of extreme price risk between selected EU milling wheat markets in the years 2005–2015. Extreme price risk (value at risk) was estimated using the ARMA-GARCH-EVT models. In turn, the risk transfer phenomenon was identified using the Granger causality in risk test according to Cheung and Ng, the Granger test in relation to logarithmic price increments exceeding values at risk and the quotient of these increments and values at risk. Results of these tests indicate the effect of extreme price risk transfer on the EU milling wheat markets in the years 2005–2015. The market from which the risk was most frequently transferred was the wheat market in France, while the wheat markets in Poland and in Germany were those, onto which the risk was most frequently transferred.

Keywords: spillover effect, Granger causality in risk, value at risk, wheat prices

JEL codes: C58, Q11

INTRODUCTION

The market for milling wheat is a major agricultural produce market in the European Union. The leading EU wheat producers include France, Germany, Great Britain and Poland. In turn, the key futures market (characterised by the greatest liquidity) for wheat in Europe is the futures market for futures contracts listed on the Euronext exchange in Paris. For the entities on the agricultural market it is essential to determine the mechanism transmitting the price risk between wheat markets due to high fluctuations in wheat prices, since extreme price variations constitute the greatest threat and chance for business entities. Extreme price risk refers to events characterised by low probability of occurrence and high losses incurred

when they take place (Jajuga, 2007). These events on the markets are caused by the release of surprising information, economic crises, natural disasters and spillover from other markets (Faldziński, 2014). Results of empirical studies indicate that wheat markets within the EU are interrelated (Rembeza, 2009; Hamulczuk and Łopaciuk, 2013; Hamulczuk, 2015). For this reason we may observe transfer of the extreme price risk between wheat markets within the EU. Studies conducted to date have analysed primarily causality between cash prices for wheat and cash and futures prices for wheat in Europe and the USA. Thus the aim of this study was to supplement research to include the analysis of extreme price risk transfer between selected milling wheat markets in the European Union.

¹ Corresponding author: Wojska Polskiego 28, 60-637 Poznań, Poland, m.just@up.poznan.pl, +4861 846 62 14

MATERIALS AND METHODS

This study used time series for average weekly milling wheat prices from selected EU countries (Integrated Agricultural Market Information System) and closing quotes for futures contracts for milling wheat from the Euronext exchange in Paris in the period from 3 January 2005 to 6 December 2015. All prices were synchronised, supplementing missing data with arithmetic means from the preceding and successive prices in relation to the missing price. The countries for analyses (France, Germany, Poland) were selected based on the volume of wheat production and availability of data on prices. Analyses were conducted on weekly percentage logarithmic increments of prices, which were established from the formula $r_t = 100 \ln(P_t / P_{t-1})$, where P_t denotes an average weekly price of wheat in time t . Considering the properties of logarithmic wheat price increments (the occurrence of autocorrelation and the effect of ARCH, leptokurtosis and skewness of distributions), the extreme price risk (values at risk) on the wheat markets were determined using the peaks over threshold approach with volatility models (ARMA-GARCH-EVT models). In turn, in order to detect the phenomenon of risk transfer the Granger test for causality in risk according to Cheung and Ng was used. In order to confirm the results of this test additionally the Granger test was applied in relation to extreme logarithmic price increments and the quotient of these increments and values at risk. The effect of lags of one and two weeks were investigated.

In order to apply causality tests we need to determine values at risk. Let X_t and Y_t denote stationary stochastic processes with discrete time and let $\mathcal{F}_{XY,t-1} = \{X_{t-j}, Y_{t-j}, j = 1, 2, \dots\}$ be a set of information available in time $t - 1$, and $\mathcal{F}_{Y,t-1} = \{Y_{t-j}, j = 1, 2, \dots\}$ will be a set of the same information excluding information on process X_t . The term value at risk (VaR) denotes the percentage loss in commodity value. Formally the value at risk at the level of tolerance α for the long (short) position in a commodity is a number opposite to the quantile of order α (quantile of order

$1 - \alpha$) for the conditional distribution Y_t (Doman and Doman, 2009): $P(Y_t \leq -VaR_{Y_t}(\alpha) | \mathcal{F}_{Y,t-1}) = \alpha$, $(P(Y_t \geq VaR_{Y_t}(1 - \alpha) | \mathcal{F}_{Y,t-1}) = \alpha)$. This paper investigated percentage logarithmic increments in wheat prices r_t . It was assumed that r_t are generated by the process (Doman and Doman, 2009) $r_t = \mu_t + \sigma_t \varepsilon_t$, where: $\mu_t = E(r_t | \mathcal{F}_{r,t-1})$, $\sigma_t^2 = \text{var}(r_t | \mathcal{F}_{r,t-1})$, $\varepsilon_t \sim iid(0,1)$. Thus VaR were expressed for the long and short positions using the respective formula:

$$VaR_{r_{t+1}}(\alpha) = -\mu_t(1) - \sigma_t(1)F_{\varepsilon_t}^{-1}(\alpha),$$

$$VaR_{r_{t+1}}(1 - \alpha) = \mu_t(1) + \sigma_t(1)F_{\varepsilon_t}^{-1}(1 - \alpha), \quad (1)$$

where:

$\mu_t(1)$, $\sigma_t(1)$ – forecasts for one period ahead, respectively, for the conditional mean and conditional standard deviation;

$F_{\varepsilon_t}^{-1}(\alpha)$, $F_{\varepsilon_t}^{-1}(1 - \alpha)$ – quantile ε_t of order α and $1 - \alpha$, respectively.

In this study respective ARMA models were fit to the conditional mean and GARCH models with Student's t -distribution or skewed Student's t -distribution for conditional standard deviation. The ARMA and GARCH models are described e.g. in Doman and Doman (2009). Next the peaks over threshold model was used to model distribution tails for standardised residuals from the GARCH model (assuming 12.5% observations to be extreme observations). This made it possible to model only distribution tails instead of entire distributions, i.e. more accurate estimation of distribution tails. A detailed description of this method (GARCH-EVT models) is presented in (McNeil and Frey, 2000). Values at risk were determined for the long and short positions in wheat (the left and right distribution tails for wheat price increments) for the level of tolerance of 0.1.

The Granger test was conducted based on the determined values at risk. In the causality concept introduced by Granger (1969) it is assumed that X_t is the Granger causality for Y_t , if current values Y_t may be estimated more accurately using past values X_t than without them (at the unchanged remainder informa-

tion) (Osińska, 2006). In the Granger test a null hypothesis is verified, in which it is assumed that X_t is not the Granger cause for Y_t in the following form (Osińska, 2006): $\sigma^2(Y_t|F_{XY,t-1}) < \sigma^2(Y_t|F_{Y,t-1})$, where σ^2 denotes variance of the prediction error. If inequality is not satisfied, X_t is the Granger cause for Y_t . Two models are estimated in this test:

$$Y_t = \alpha_0 + \sum_{j=1}^k \alpha_j Y_{t-j} + \sum_{j=1}^k \beta_j X_{t-j} + \eta_t,$$

$$Y_t = \alpha_0 + \sum_{j=1}^k \alpha_j Y_{t-j} + \varepsilon_t, \quad (2)$$

where:

- $\alpha_0, \alpha_j, \beta_j$ – parameters of the model;
- η_t, ε_t – random components;
- k – order of lag.

The next stage consists in the verification of the null hypothesis that all coefficients β_j are equal to zero, which corresponds to the hypothesis on a lack of Granger causality. In this study linear regression models were estimated for extreme logarithmic wheat price increments on a given market. The price increments exceeding values at risk ($Y_t \leq -VaR_{Y_t}(\alpha)$, $Y_t \geq VaR_{Y_t}(1-\alpha)$) were considered extreme logarithmic price increments, while the other observations were ascribed the zero value. The test variant with the Fisher-Snedecor statistic was applied (Osińska, 2006):

$$F = \frac{(S^2(\varepsilon_t) - S^2(\eta_t))/k}{S^2(\eta_t)/(T - 2k - 1)}, \quad (3)$$

where:

- $S^2(\eta_t), S^2(\varepsilon_t)$ – square sum of residuals for the models presented in equation (2);
- T – sample size.

At the correctness of the null hypothesis the F statistic has the Fisher-Snedecor distribution with k and $T - 2k - 1$ degrees of freedom.

In the next stage of the study the Granger causality in risk test was conducted. The concept was introduced by Hong, Liu and Wang (2009). The occurrence of the Granger causality in risk means that the

presence of high risk on one market makes it possible to more accurately estimate the occurrence of a similar risk on another market. This paper verifies the null hypothesis that X_t is not the Granger cause in risk for Y_t of the form (Hong, Liu and Wang, 2009):

$$E(I_{Y,t}|F_{Y,t-1}) = E(I_{Y,t}|F_{XY,t-1}), \quad (4)$$

where $I_{Y,t}$ denotes the indicator function, which for the long or short positions in the commodity assumes the value of one, respectively, when the logarithmic price increments exceed values at risk, while otherwise it takes the value of zero. When equation (4) is not met X_t is the Granger cause in risk for Y_t . This study was conducted using the Granger causality in risk test according to Cheung and Ng (1996):

$$CHN = T \sum_{j=1}^k r^2(j), \quad (5)$$

where:

- T – sample size;
- $r(j)$ – estimator of the coefficient of cross-correlation $\rho(j)$ between $I_{X,t}$ and $I_{Y,t}$;
- k – the order of delay.

The CHN statistic for the correct null hypothesis takes the distribution convergent to $\chi^2(k)$.

RESULTS AND DISCUSSION

It is generally accepted that the method to determine values at risk provides good estimations when the number of exceedances of the estimated value at risk by empirical logarithmic price increments is consistent with the assumed level and the distribution of exceedances is uniform. The quality of estimations for the value at risk for logarithmic wheat price increments for the level of tolerance equal to 0.1 was evaluated using the Kupiec test (Kupiec, 1995), Christoffersen test (Christoffersen, 1998), Christoffersen and Pelletier test (Christoffersen and Pelletier, 2004). Results of these tests are presented in Table 1. Taking into consideration the results of the three tests it may be stated that all the estimations of values at risk were of good quality. The share of exceedances was close to the assumed level and the exceedances were uniformly distributed.

Table 1. The evaluation of the VaR estimation quality

Item	Germany		France		Poland		Euronext in Paris	
	Left tail	Right tail	Left tail	Right tail	Left tail	Right tail	Left tail	Right tail
ET	57	57	57	57	57	57	57	57
T_1	52	56	62	56	58	60	61	63
LR_UC	0.481	0.016	0.495	0.016	0.023	0.185	0.321	0.705
p-value	0.488	0.900	0.482	0.900	0.878	0.667	0.571	0.401
LR_CC	2.742	0.066	0.579	0.473	0.305	2.805	3.617	0.884
p-value	0.254	0.968	0.749	0.789	0.858	0.246	0.164	0.643
LR_D	0.423	0.102	0.829	0.457	0.083	3.836	0.023	1.500
p-value	0.516	0.750	0.363	0.499	0.773	0.050	0.879	0.221

ET (T_1) – the expected (empirical) number of exceedances of the estimated VaR by the actual logarithmic prices increments; LR_UC (LR_CC, LR_D) – Kupiec (Christoffersen, Christoffersen and Pelletier) test statistic; in bold grey font – rejection of the null hypothesis Kupiec test: the share of VaR violations by actual logarithmic prices increments is compliant with an assumed α (Christoffersen test: the share of VaR hits by actual logarithmic prices increments is compliant with an assumed α and the exceedances are independent – the first hit; Christoffersen and Pelletier test: the duration of time (in weeks) between the violations of VaR by actual logarithmic prices increments is independent) for the significance level of 0.1.

Source: own study.

Table 2 presents results of the Cheung and Ng test for the wheat long and short positions for delays of one and two weeks, respectively. Irrespective of the position occupied on the wheat market, the hypothesis on a lack of the Granger causality in risk for lags of one and two weeks for the pairs of wheat in France–wheat in Germany; wheat in France–wheat futures at the Euronext exchange; wheat futures at the Euronext exchange–wheat in Germany was rejected (at the level of significance of 0.05). In view of the fact that the analysed test ascribes identical weights to all the delays we need to state that significant correlation coefficients are indicated by considerable fluctuations in the test statistic. This means that the extreme price risk was transferred from the wheat market in France to the wheat market in Germany for lags amounting to one and two weeks, while it was transferred to the market of futures listed at the Euronext exchange only for the 1-week lag. The wheat market in Germany was the recipient of risk from the wheat futures market in Paris for lags of one and two weeks. Moreover, it was found that the wheat market in Poland was the recipient of risk from the wheat

market in Germany in the case of extreme price hikes and from the wheat market in France in the case of extreme price drops for the 1-week lags.

Results of the Granger test conducted for the extreme logarithmic wheat price increments and the quotient of these increments and values at risk are presented in Table 3. Results of these tests confirmed the existence of the Granger causality in relation to extreme price reductions and hikes for the following pairs: wheat in France–wheat in Germany; wheat in France–wheat futures on the Euronext exchange; wheat futures on the Euronext exchange–wheat in Germany; wheat in Germany–wheat in Poland in the case of extreme price hikes. Additional tests indicated that extreme wheat price hikes on the cash and futures markets in France and extreme price reductions for wheat in Germany may have been the Granger causality for extreme hikes and reductions in wheat prices in Poland.

Generally it may be observed that the transmission of risk on the wheat market in Poland was observed more often in the case of short positions. In view of the fact that average wheat wholesale prices for wheat

Table 2. Results of the Cheung and Ng test

Item	Lag	Left tail		Right tail	
		1	2	1	2
~F->G	CHN	29.890	36.736	34.773	39.235
	p-value	0.000	0.000	0.000	0.000
~G->F	CHN	0.382	1.550	1.419	1.482
	p-value	0.536	0.461	0.234	0.477
~F->P	CHN	6.683	6.799	0.913	1.817
	p-value	0.010	0.033	0.339	0.403
~P->F	CHN	0.010	1.549	1.786	1.787
	p-value	0.921	0.461	0.181	0.409
~F->E	CHN	51.929	52.326	63.681	63.691
	p-value	0.000	0.000	0.000	0.000
~E->F	CHN	0.520	2.619	0.125	0.135
	p-value	0.471	0.270	0.723	0.935
~G->P	CHN	1.674	1.781	7.777	7.778
	p-value	0.196	0.410	0.005	0.020
~P->G	CHN	0.186	5.864	1.999	2.000
	p-value	0.666	0.053	0.157	0.368
~G->E	CHN	1.291	1.728	0.009	0.131
	p-value	0.256	0.421	0.924	0.937
~E->G	CHN	9.578	12.358	23.424	26.297
	p-value	0.002	0.002	0.000	0.000
~P->E	CHN	1.689	1.692	1.041	2.072
	p-value	0.194	0.429	0.308	0.355
~E->P	CHN	1.541	1.552	2.118	2.644
	p-value	0.214	0.460	0.146	0.267

F (G, P, E) – logarithmic increases in prices of wheat in France (in Germany, in Poland, contracts on the Euronext exchange); in bold black (grey) font – rejection of the null hypothesis on the lack of Granger causality in risk for the significance level of 0.05 (0.1).

Source: own study.

Table 3. Results of the Granger test

Item	Lag	Variant with extreme prices increments				Variant with the quotient of extreme prices increments and VaR			
		Left tail		Right tail		Left tail		Right tail	
		1	2	1	2	1	2	1	2
~F->G	F	36.282	22.979	29.160	20.554	35.290	21.138	20.616	20.110
	p-value	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000
~G->F	F	0.875	0.911	1.409	2.118	0.571	1.104	1.189	0.405
	p-value	0.350	0.403	0.236	0.121	0.450	0.332	0.276	0.667
~F->P	F	1.075	0.537	6.374	5.460	3.336	1.907	1.745	6.885
	p-value	0.300	0.585	0.012	0.004	0.068	0.149	0.187	0.001
~P->F	F	0.160	0.075	0.513	0.380	0.027	0.081	1.651	0.772
	p-value	0.689	0.928	0.474	0.684	0.869	0.923	0.199	0.463
~F->E	F	98.306	48.873	264.331	132.933	63.031	31.348	140.400	70.175
	p-value	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000
~E->F	F	0.873	1.783	1.594	2.952	0.010	1.079	0.150	0.126
	p-value	0.351	0.169	0.207	0.053	0.922	0.341	0.699	0.882
~G->P	F	2.597	6.984	20.992	10.133	0.688	7.724	13.374	6.782
	p-value	0.108	0.001	0.000	0.000	0.407	0.000	0.000	0.001
~P->G	F	0.207	1.054	2.706	2.815	0.013	0.917	0.462	1.027
	p-value	0.649	0.349	0.101	0.061	0.908	0.400	0.497	0.359
~G->E	F	1.889	1.027	6.273	3.863	0.891	0.488	1.305	0.835
	p-value	0.170	0.359	0.013	0.022	0.346	0.614	0.254	0.435
~E->G	F	3.329	4.137	30.100	15.083	6.025	4.767	26.986	14.518
	p-value	0.069	0.016	0.000	0.000	0.014	0.009	0.000	0.000
~P->E	F	1.387	1.186	1.927	1.086	1.714	0.917	1.301	0.799
	p-value	0.239	0.306	0.166	0.338	0.191	0.400	0.254	0.450
~E->P	F	0.021	0.022	6.102	2.845	2.261	1.237	11.760	5.951
	p-value	0.884	0.978	0.014	0.059	0.133	0.291	0.001	0.003

F (G, P, E) – logarithmic increases in prices of wheat in France (in Germany, in Poland, contracts on the Euronext exchange); in bold black (grey) font – rejection of the null hypothesis on the lack of Granger causality for the significance level of 0.05 (0.1).

Source: own study.

purchased by companies in Poland were considered here, we may infer that 'adverse' events (for purchasing entities) with limited probability of their occurrence are more frequently transferred between markets. Moreover, it may be inferred that risk transfer occurs from larger wheat markets to smaller ones.

CONCLUSIONS

The results of the presented tests showed the occurrence of the effect of extreme price risk transfer on milling wheat markets in the European Union in the years 2005–2015. The wheat market in France was the market, from which risk was transferred most frequently, while markets, onto which risk was transmitted were wheat markets in Poland and in Germany. The study covered the period of drastic hikes and drops of wheat and futures contracts for wheat prices during the economic and financial crisis. The study should therefore be extended for the next years. The obtained information on the mechanism of extreme risk spillover on the EU wheat markets may be applied to provide more accurate estimations of the extreme wheat price risk.

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